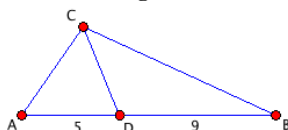


In our Level B class, students are expected to have completed an equivalent of two years of high school, and have a solid understanding of algebra, geometry, and elementary number theory. Experience with problem solving, such as prior NYMC or math team participation, is desirable but not required.

Topics include algebra, geometry, number theory, combinatorics, probability, induction, recursion, polynomials, and inequalities. The problems can be difficult, but hopefully they're also interesting and fun. Here are some sample problems.

Problems that you ought to be able to solve before taking this class

1. What is the ratio of the area of the triangle DBC to the area of the triangle ADC ?



2. How many positive whole numbers less than or equal to 1,200 are multiples of 2 or 3?
3. How many 5 digit numbers can be formed using each of the digits 0, 2, 4, 6, and 8 exactly once?
4. The quadratic polynomial equation $x^2 + 2kx + 3k = 0$ has exactly one root. What are the possible values of k ?

Examples of interesting problems that we'll consider in this class

1. How many zeros are at the end of $1000!$?
2. 9 girls and 3 boys sit in one row of a classroom. How many seating arrangements are there, if none of the boys are allowed to sit next to each other?
3. Find the smallest n such that the n^{th} Fibonacci number is divisible by 30.
4. The polynomial $P(x)$ has remainder 3 when divided by $x - 1$ and remainder 5 when divided by $x + 1$. What is the remainder when $P(x)$ is divided by $x^2 - 1$?
5. A gecko and an anti-gecko take a random walk on the faces of a cube, starting on opposite faces. How long, on average, will it be before the geckos walk onto the same face of the cube and annihilate each other?
6. A penguin takes a random walk on a long ladder, starting at the intersection of one of the rungs and one of the sides. Every second she moves, with equal probability, either to the other side of the ladder (on the same rung) or up or down one rung (on the same side). However, she only moves up on one side of the ladder, and she only moves down on the other side. Find the probability that, after one minute, the penguin is back where she started.
7. Given a circle, two points on the circle, and a segment of some fixed length, construct a pair of parallel chords, one chord through each of the given points, such that the sum of the lengths of the chords is equal to the length of the given segment.
8. Prove Nesbitt's inequality, for a , b , and c positive real numbers:

$$\frac{a}{b+c} + \frac{b}{c+a} + \frac{c}{a+b} \geq \frac{3}{2}$$